Unprovability and Beyond

There are a large number of open conjectures that resist repeated attempts from the most brilliant human brains, and one nature worry is that, could any of these conjectures be actually unprovable from the current axiom system, for example ZFC? If so, then the next natural question would be, how can we prove that a statement is unprovable? In this talk we investigate and try to understand a deeper incompleteness phenomenon that "being unprovable" could be arbitrarily hard to prove, and we bring such phenomenon into higher levels that an analogous result holds after adding all truths of bounded quantifier complexity into the base theory.